# Password-Based Cryptography: Strong Security from Weak Secrets 

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## ROADMAP

- Password-Based Authentication

How to make password checking systems even better

- Password-Authenticated Secret Sharing

How to make cryptography accessible to end users

## Password-Based Authentication

- Most prominent form of user authentication - convenient! No key, software, ...


Password rules:

$$
h=\operatorname{Hash}(p w d)
$$

upper and lower case letters and numbers at least
16 characters in length
vs. 4-digit PIN for ATM cards
never reuse your password on another site
change your passwords periodically
why the difference?
the ATM will retain the card after 3 failed attempts!

## Password-Based Authentication

- If service provider is trusted \& throttles after too many failed attempts
$\rightarrow$ short passwords are sufficient!
- But main threat to password security is server compromise

$h^{\prime}=h$ ?
stores only (salted) password hashes

$$
h=\operatorname{Hash}(p w d)
$$

## DICTIONARY ATTACK!



Passwords inherently insecure?
No! We're just using them incorrectly ...

## Password-Based Authentication Done Right

- Offline attacks are inherent in single-server setting
- Solution: split password verification over multiple servers



## Pythia: OPRF Service

- Replace Hash by a secure $\operatorname{PRF}(\square$, $p w d$ )
- Store at remote server \& evaluate PRF obliviously



## Distributed Password Verification | High-Level Idea

- Replace Hash by a secure $\operatorname{PRF}(\square$, $p w d)$
- Split secret key $\quad$ into $n$ shares
- $h=\operatorname{PRF}(\bigcirc \quad, p w d)$ computed distributed:
- Servers don't learn anything about pwd or $h$

| Username | Hash |
| :--- | :--- |
| Alice | wb3822Ujsd4 |
| Bob | b5kMsa8dsbn |
| Carol | 77peCu52Kry |



Jointly compute


## Distributed Password Verification | Security

- Secret key has high-entropy, i.e., cannot be guessed
$\rightarrow$ Adversary needs backend servers (or full key) to verify password guesses
$\rightarrow$ Backend servers will stop verification if activity is suspicious



## Distributed Password Verification | Proactive Security

- Secret key $\quad$ gets re-shared periodically
$\rightarrow$ All previous key shares get useless
$\rightarrow$ Adversary must break into all servers at the same time
- As long as one server is not corrupted
$\rightarrow$ Passwords are secure



## DPV Protocol

Optimal Distributed Password Verification. ACM CCS'15.
Camenisch, Lehmann, Neven.

## Distributed Password Verification | Protocol

- Replace Hash by a secure $\quad H(\text { uid, } p w d)^{k} \quad \mathrm{k}=$ random element in Zq
- Split secret key $k=k_{1}+k_{2}+\ldots+k_{n} \bmod q$ Cyclic group of prime order q



## Distributed Password Verification | Protocol

- Replace Hash by a secure $H(u i d, p w d)^{k}$
- Split secret key $k=k_{1}+k_{2}+\ldots+k_{n} \bmod q$



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$$
\begin{aligned}
& \xrightarrow{\text { uid, } p w d} \underset{\substack{\text { Service } \\
\text { Provider }}}{U=H(u i d, p w d)^{N}} \\
& \begin{aligned}
& \text { random } N \text { in } Z_{q} \\
& V=\prod_{i}^{1 / N}=U^{k_{1}+k_{2}+\ldots+k_{n}} \\
&=H(u i d, p w d)^{k} \\
& h=H^{\prime}(u i d, p w d, V)
\end{aligned}
\end{aligned}
$$

## Distributed Password Verification | Protocol

- Replace Hash by a secure $H(u i d, p w d)^{k}$
- Split secret key $k=k_{1}+k_{2}+\ldots+k_{n} \bmod q$
Backend
Server 1 $k_{1}$ + blinding for adaptive security


Service
Provider


Backend
Server 2 $k_{2}$
random $N$ in $Z_{q}$

$$
U=H(u i d, p w d)^{N}
$$

+ pairing for correctness $\quad{ }^{1 / k_{1}+k_{2}+\ldots+k_{n}}$

$$
\begin{aligned}
& =H(u i d, p w d)^{n} \\
h & =H^{\prime}(u i d, p w d, V)
\end{aligned}
$$

## Distributed Password Verification | Protocol

- Proactive security \& re-sharing of keys:

Agree on pseudorandom shares of zero:
$\delta_{1}+\delta_{2}+\ldots+\delta_{n}=0 \bmod q$

$$
k_{1}^{\prime}=k_{1}+\delta_{1}
$$

$$
k_{2}^{\prime}=k_{2}+\delta_{2}
$$

$$
k_{n}^{\prime}=k_{n}+\delta_{n}
$$

## Distributed Password Verification = Distributed OPRF (Oblivious PRF)

compute $y=\operatorname{PRF}(k, x)$ in a blind $\&$ distributed manner


## Distributed Password Verification <br> = Distributed OPRF (Oblivious PRF)

compute $y=\operatorname{PRF}(k, x)$ in a blind $\&$ distributed manner

$$
\begin{aligned}
& k=\operatorname{KGen}(\tau) \\
& k_{1}+k_{2}+\ldots+k_{n}=\operatorname{Share}(k, n)
\end{aligned}
$$



## Distributed Password Verification | Security \& Efficiency

- Efficient \& round-optimal protocol
- 1 round of communication
- Login: one exponentiation per server (two for SP)
- Non-interactive key refresh
- Prototype implementation \& evaluation (Ergon)
- 3 backend servers, each $16 \times 2.9$ Ghz core: 285 logins/second
- Provable security in very strong security model
- Adaptive \& active adversaries, UC Framework
- One-More Gap DH (OMGDH), Random Oracle
- Password protection back where it belongs: on the server !



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## How to bridge cryptographic keys \& humans

- Most cryptography relies on strong secret keys
- Easy to manage for servers and devices ... not so easy for humans

- 

----BEGIN PRIVATE KEY----
MIICXgIBAAKBgQDHikastc8+181zCg/qWW8dMr8mqvXQ3qbPAmuORjxoZVI47tvs kYIFAXOfOsPrhO2nUuooJngnHV0639iTTEYG1vckNaW2R6U5QTdQ5Rq5u+uV3pMk 7w7Vs4n3urQ6jnqt2rTXbC1DNa/PFeAZatbf7ffBByOIGOOzc128IshYcwIDAQAB AoGBALTNI2JxTvq4SDW/3VHOfZkQXWH1MM10oeMbB2qO5beWb11FGaOO77nGKfWc bYgfp5Ogrql4yhBvLAXnxH8bcqqwORtFhlyV68U1y4R+8WxDNhOaevxH8hRS/1X5 031DJm1JIUOE+vStiktNOtC3ebH5hE+1OxbIHSZ+WOWLYX7JAkEA5uigRgKp8ScG auUijvdOLZIhHWq7y5Wz+nOHUuDw8P7wOTKU34QJAoWEe771p9Pf/GTA/krOBQnP QvWUDxGzJwJBANO5C6krwPeryFKrKtjOGJIniloY72wRnoNcdEEs3HDRhf48YWFo riRbZylzzzNFy/gmzT6XJQTfktGqq+FZD9UCQGIJaGrxHJgfmpDuAhMzGsUsYtTr iRox0D1Iqa7dhE693t5aBG0100F6MLqdZA1CXrn5SRtuVVaCSLZEL/2J5UcCQQDA d3MXucNnN4NPuS/L9HMYJWD7IPoosaORcgyK77bSSNgk+u9WSjbH1uYIAIPSffUZ bti+jc1dUg5wb+aeZlgJAkEAurrpmpqj5vg087ZngKfFGR5rozDiTsK5DceTV97K a3Y+Nzl+XWTxDBWk4YPh2ZIKv402hZEfWBYxUDn5ZkH/bw==
------END PRIVATE KEY-----

E.g., encrypted cloud storage (untrusted cloud)

How to store the secret key?

- Access from many devices
- Trusted hardware inconvenient
- Device(s) can get broken or lost


## Secret Sharing | Shamir’ 79

user shares secret $K$ with $n$ servers

user retrieves $K$ from at least $t+1$ servers

$\mathrm{t}+1$ shares needed to reconstruct $K$
if at most t servers are corrupt $\rightarrow$ they don't learn anything about $K$

## Password-Authenticated Secret Sharing | BJSL’11

user shares secret $K$ with n servers protected by password p

user retrieves $K$ from at least $t+1$ servers using password p'

$\mathrm{t}+1$ shares needed to reconstruct $K$ and to verify whether $p=p^{\prime}$
if at most $t$ servers are corrupt $\rightarrow$ they don't learn anything about $K$ or can offline attack $p$ honest server throttle verification after too many (failed) attempts

## Password-Authenticated Secret Sharing (TPASS/PPSS)

user shares secret $K$ with n servers protected by password $p$

user retrieves $K$ from at least $t+1$ servers using password p’

user has to remember the servers she trusted at setup

## Password-Authenticated Secret Sharing (TPASS/PPSS)

user shares secret $K$ with $n$ servers protected by password $p$

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[CLLN'14] Camenisch, Lehmann, Lysyanskaya, Neven.
Memento: How to Reconstruct your Secrets from a Single Password in a Hostile Environment. Crypto 2014

## Overview of TPASS Solutions

| Scheme | Security Model | Assumption | Retrieval |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Rounds | Expon User | tiation Server |
| BJSL'11 | Game | DDH-ROM | 3 | $8 \mathrm{t}+17$ | 16 |
| CLLN'14 | UC | DDH-ROM | 5 | 14t+24 | $7 \mathrm{t}+28$ |
| JKK'14 | Game | OMGDH-ROM | 1 | $2 \mathrm{t}+3$ | 3 |
| ACNP'16 | Game | OMGDH-ROM | 1 | ? | ? |
| JKKX'16 | UC | OMGDH-ROM | 1 | t+2 | 1 |
| JKKX'17 | UC | TOMGDH-ROM | 1 | 2 | 1 |

## SECURITY MODELS

for password-based crypto

## Provable Security

## Trust me -

 I'm secure!- Old days: security by obscurity
- Now: provable security = gold standard in cryptography
- Formal security model \& formal security proof
- Also crucial for higher-level protocols: secure building blocks $\boldsymbol{\Delta}$ secure protocol


## Game-Based



## Challenge: Security Model including the User

- Game-based security notions most common
- Oracle access to some secret key function
- Secure if $\forall A d v$ : Prob[attack] = negligible




## Model

Reality

Passwords chosen at random from known, independent distribution

Honest user always uses correct password

People reuse passwords, leak info about passwords

Users make typos, "mix" passwords

## Universal Composability Framework | Canetti’00

- Security defined via ideal functionality $\mathcal{F}-\mathcal{F}$ is "secure-by-design"



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## Universal Composability Framework | Canetti’00

- Security defined via ideal functionality $\mathcal{F}-\mathcal{F}$ is "secure-by-design"
- Protocol $\pi$ securely implements $\mathcal{F}$ if $\forall A d v \exists$ Sim such that $\forall E: R E A L_{\pi, A, E} \approx I D E A L_{F, S, E}$ environment chooses passwords of honest users
$\rightarrow$ no assumptions on pwd distributions \& typos by honest users covered


Real world


Ideal world

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| Disclaimer: se | ity models | ry |  |  |  |

## TPASS by JKKX’17 | Slightly Different Setting

user shares secret $K$ with $n$ servers protected by password $p$

user retrieves $K$ from at least $t+1$ servers using password p’

user obtains a random key $K$ at setup
if $<t+1$ servers are corrupt $\rightarrow$ they don't learn anything about $K$
if $\geq t+1$ servers are corrupt $\rightarrow$ they learn $K$ (but its still a random key)

## Building Block: Threshold OPRF (T-OPRF)

compute $y=\operatorname{PRF}(k, x)$ in a blind \& distributed threshold manner
$k=\operatorname{KGen}(\tau)$
$k_{1}+k_{2}+\ldots+k_{n}=\operatorname{Share}(k$, any $t+1$ shares are sufficient to compute P

s.t. $y=\operatorname{PRF}(k, x)$


## TPASS Protocol | Setup

- user obtains secret $K$ protected by password $p$ with $n$ servers $S S=S_{1}, S_{2}, \ldots, S_{n}$

$k=\operatorname{PRF} . \operatorname{KGen}(\tau)$
$\left(k_{1}, k_{2}, \ldots, k_{n}\right)=\operatorname{Share}(k, t, n)$
if ack from all $S$ in $S S$
compute $y=\operatorname{PRF}(k, p)$
compute $h=\mathrm{H}(y)$
parse $h=(C, K)$



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if ack from all $S$ in $S S$ compute $y=\operatorname{PRF}(k, p)$
compute $h=\mathrm{H}(y)$
parse $h=(C, K)$

send $C$ to all $S$ \& output $K$


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- user obtains secret $K$ protected by password $p$ with $n$ servers $S S=S_{1}, S_{2}, \ldots, S_{n}$

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if ack from all $S$ in $S S$ compute $y=\operatorname{PRF}(k, p)$
compute $h=\mathrm{H}(y)$ parse $h=(C, K)$
send $C$ to all $S$ \& out

$K$ is always a random key
If <t+1 servers are corrupt: Adv learns nothing about $(p, K)$ If $\geq t+1$ servers are corrupt: Adv can offline attack $(p, K)$


## TPASS Protocol | Retrieval

- user retrieve her secret using password p' from $t+1$


## each $S_{i}$ :

check that $S R \subset S S$
compute $\overline{y_{i}}=\operatorname{pPRF}\left(k_{i}, \bar{x}\right)$ servers $S R=S^{\prime}{ }_{1}, S^{\prime}{ }_{2}, \ldots, S^{\prime}{ }_{t+1}$

$\bar{x}=\operatorname{Blind}\left(p^{\prime}\right)$

## TPASS Protocol | Retrieval

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check that $S R \subset S S$
compute $\overline{y_{i}}=\operatorname{pPRF}\left(k_{i}, \bar{x}\right)$

- user retrieve her secret using password pwd' from t+1 servers $S R=S^{\prime}{ }_{1}, S^{\prime}{ }_{2}, \ldots, S^{\prime}{ }_{t+1}$

$\bar{x}=\operatorname{Blind}\left(p^{\prime}\right)$
if $\left(C, \overline{y_{i}}\right)$ from all $S$ in $S R$
compute $\bar{y}=\operatorname{Comb}\left(\bar{y}_{1}, \bar{y}_{2}, \ldots, \bar{y}_{t+1}\right)$
compute $y=\operatorname{Unblind}(\bar{y})$
compute $h=\mathrm{H}(y)$ parse $h=\left(C^{\prime}, K^{\prime}\right)$
if $C^{\prime}=C$ output $K^{\prime}$ else output $K^{\prime}=\perp$


Security based on T-OPRF \& ROM
Efficient T-OPRF from OMGDH \& ROM (similar to our DORPF)

## TPASS Protocol | Retrieval

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if $C^{\prime}=C$ output $K^{\prime}$
else output $K^{\prime}=\perp$


## TPASS | Applications

- TPASS allows users to reconstruct strong secret key from weak password
- Does not require trusted storage

- Allows to bootstrap any cryptographic operation based on a strong key
- Encrypted cloud storage, strong authentication, ...
" Bootstrap strong "passwords" from K, pwd= H(K,"iacr.org")
- Reconstruction of secret key can be security risk - malware on device
- Less flexible, but more secure: protocols for joint password-based computations
- Number of "solutions", most are vulnerable against offline attacks *
- Distributed signing [CLNS16] - "Virtual Smartcard"


## Password-Based Crypto | Summary

- Passwords are convenient \& easy to use
- Low entropy makes them vulnerable to offline attacks
- Strong security from passwords requires multi-server solutions
- Prevents offline attacks \& detect online attacks
- UC-based definitions capture password use better than game-based models
- Highly-efficient solutions exist for a number of password-based primitives
- Lots of open research problems - Lets make crypto for people! ©


## Thanks! Questions?

